

## Emission index problem

Thursday, December 7, 2017 11:56 AM

A spark ignition engine is running on a dynamometer test stand and the following measurements of the exhaust products are made:

$$\text{CO}_2 = 12.47\%$$

$$\text{CO} = 0.12\%$$

$$\text{O}_2 = 2.3\%$$

$$\text{C}_6\text{H}_{14}(\text{equivalent}) = 367 \text{ ppm}$$

$$\text{NO} = 76 \text{ ppm}$$

All concentrations are by volume on a dry basis. The engine is fueled by iso-octane ( $\text{C}_8\text{H}_{18}$ , MW = 114.2 kg/kmol). Determine the emission index of the unburned hydrocarbons expressed as equivalent hexane.  $\text{MW}_{\text{C}_6\text{H}_{14}} = 86.2 \text{ kg/kmol}$ .

$$\begin{aligned} EI_{\text{C}_6\text{H}_{14}} &= \left( \frac{X_{\text{C}_6\text{H}_{14}}}{X_{\text{CO}} + X_{\text{CO}_2}} \right) \left( \frac{x \text{ MW}_{\text{C}_6\text{H}_{14}}}{\text{MW}_{\text{C}_8\text{H}_{18}}} \right) \\ &= \left( \frac{367 \times 10^{-6}}{0.0012 + 0.1247} \right) \left( \frac{8 (86.2)}{114.2} \right) \end{aligned}$$

$$\begin{aligned} &= 0.0176 \text{ kg/kg} \text{ or } 17.6 \text{ g/kg} \\ EI_{\text{C}_6\text{H}_{14}} &= \left( \frac{X_{\text{C}_6\text{H}_{14}}}{X_{\text{CO}} + X_{\text{CO}_2} + C X_{\text{C}_6\text{H}_{14}}} \right) \left( \frac{8 (86.2)}{114.2} \right) \\ &= \left( \frac{367 \times 10^{-6}}{0.0012 + 0.1247 + C(367 \times 10^{-6})} \right) \left( \frac{8 (86.2)}{114.2} \right) \\ &= 0.0173 \text{ kg/kg} \quad 17.3 \text{ g/kg} \end{aligned}$$

## Corrected Concentration Problem

Thursday, December 7, 2017 12:03 PM

A spark ignition engine is running on a dynamometer test stand and the following measurements of the exhaust products are made:

- CO<sub>2</sub> = 12.47%
- CO = 0.12%
- O<sub>2</sub> = 2.3%
- C<sub>6</sub>H<sub>14</sub>(equivalent) = 367 ppm
- NO = 76 ppm

All concentrations are by volume on a dry basis. The engine is fueled by iso-octane (C<sub>8</sub>H<sub>18</sub>, MW = 114.2 kg/kmol).

- A) Convert the given NO concentration to a wet basis, and
- B) What is the NO concentration corrected to 5% O<sub>2</sub>?

$$A) \quad X_{NO, wet} = X_{NO, dry} \frac{N_{mix, dry}}{N_{mix, wet}}$$

$$\frac{N_{mix, dry}}{N_{mix, wet}} = 1 + \frac{y}{z(4.76a - y/4)} = 1.146$$

$$a = \frac{x + (1 - x_{O_2, dry}) y/4}{1 - 4.76 x_{O_2, dry}}$$

$$= \frac{8 + (1 - 0.023) 18/4}{1 - 4.76(0.023)} = 13.92$$

$$X_{NO, wet} = X_{NO, dry} \frac{N_{mix, dry}}{N_{mix, wet}} = \frac{76 \text{ ppm}}{1.146} = 66.3 \text{ ppm}$$

$$B) \quad N_{mix @ 2\% O_2} = 4.76 \left[ \frac{x + (1 - x_{O_2}) y/4}{1 - 4.76 x_{O_2}} \right] - \frac{y}{4}$$

$$N_{mix @ 2.3\% O_2} = 4.76 \left[ \frac{8 + (1 - 0.023) \frac{18}{4}}{1 - 4.76(0.023)} \right] - \frac{18}{4}$$

$$\approx 61.76$$

$$N_{mix @ 5\% O_2} = 4.76 \left[ \frac{8 + (1 - 0.05) \frac{18}{4}}{1 - 4.76(0.05)} \right] - \frac{18}{4}$$

$$= 72.18$$

$$X_{NO @ 5\% O_2} = X_{NO @ 2.3\% O_2} \frac{N_{mix @ 2.3\% O_2}}{N_{mix @ 5\% O_2}}$$

$$= 76 \text{ ppm} \left( \frac{61.74}{72.18} \right)$$

$$= 65 \text{ ppm}$$