

Solid Fuel Combustion

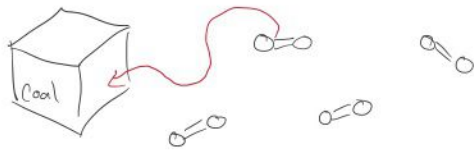
Tuesday, November 14, 2017 3:04 PM

2 rxn mechanisms:

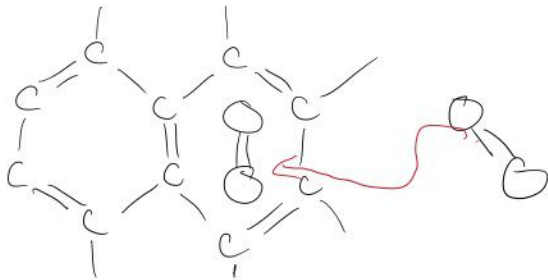
1) Catalysis

homogeneous rxns: rxns that occur in a single phase

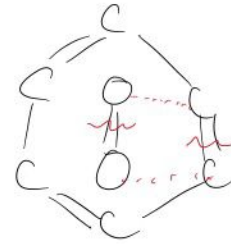
heterogeneous rxns: rxns that occur over 2 physical states. e.g. gas-liquid, gas-solid



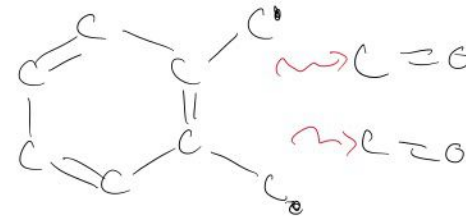
1) transport of rxn molecule to the surface by convection and/or diffusion



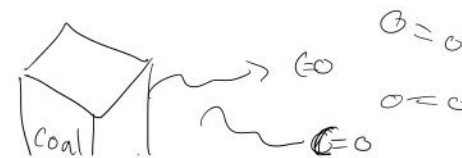
2) adsorption of the rxn molecule on surface



3) elementary rxn steps involving combos of adsorbed molecules, the surface, & gas molecules



4) desorption of product molecules from surface



LV

$0 < C$

5) transport of product molecules from surface by convection and/or diffusion

rate laws:

if rxn A is weakly adsorbed

$$R = k(T) [A]$$

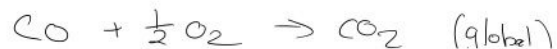
if rxn A is strongly adsorbed

$$R = k(T)$$

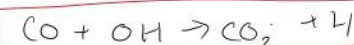
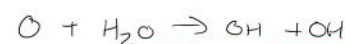
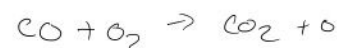
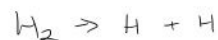
if rxn A is weakly adsorbed
AND product B is strongly adsorbed

$$R = k(T) \frac{[A]}{[B]}$$

carbon burns via



elementary steps



ΔH_f (kJ/kmol)

$$CO_2 \quad -393546$$

$$CO \quad -110541$$

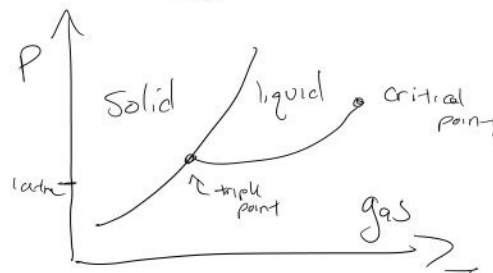
$$OH \quad 38985$$

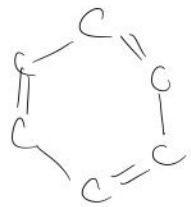
$$H \quad 217977$$

$$\Delta H_{rxn} = -104613$$

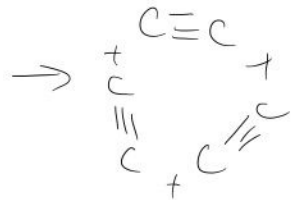
kJ/kmol

2) pyrolysis

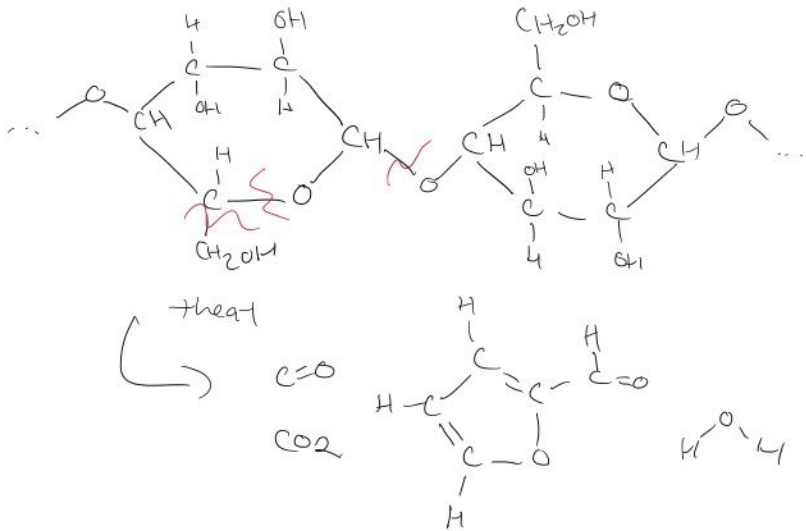




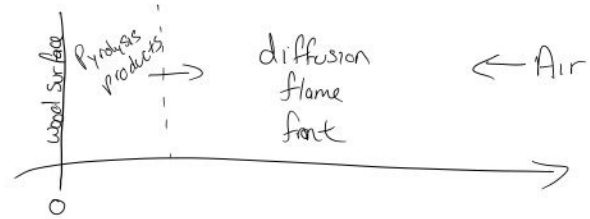
+ heat



for wood:



Air



One-film model

Assumptions

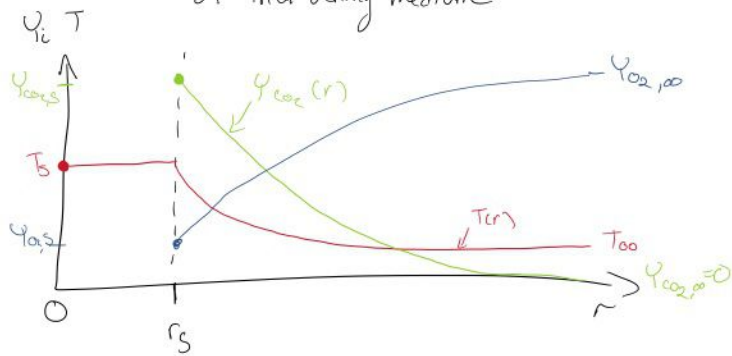
- 1) burning process is quasi-steady
- 2) spherical carbon particles burning in a quiescent, infinite ambient medium that only contains O_2 & inert gas. No interactions w/ other particles. no convection
- 3) Carbon reacts w/ O_2 to produce CO_2 ($C + O_2 \rightarrow CO_2$).
- 4) gas phase only has O_2 , CO_2 & inerts. O_2 diffuses inward. CO_2 diffuses outward. inerts form stagnant layer (Stefan problem)

5) k, c_p, ρ, D_{AB} all constant

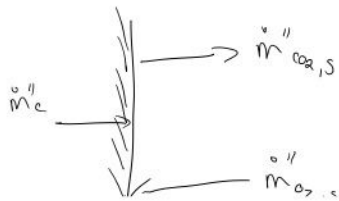
$$Le = k / (\rho c_p D) = 1$$

6) carbon particle impervious to gas

7) particle has uniform T & radiates as a grey body to surroundings w/o participation of intervening medium

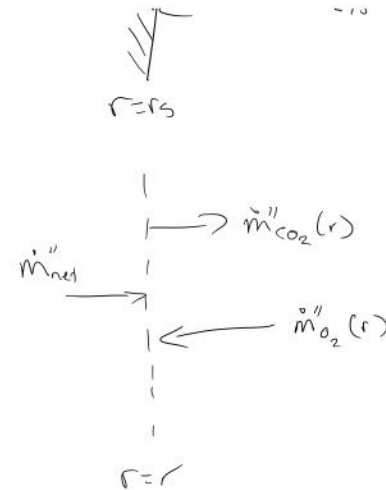


Mass : species conservation



@ surface

$$\dot{m}_c'' = \dot{m}_{CO_2}'' - \dot{m}_{O_2}''$$



@ $r > r_s$

$$\dot{m}_{net}''(r) = \dot{m}_{CO_2}'' - \dot{m}_{O_2}''$$

mass flow is const.

$$\dot{m}_{c,s}'' = \frac{\dot{m}_c}{4\pi r_s^2} = \frac{\dot{m}_{CO_2}}{4\pi r_s^2} - \frac{\dot{m}_{O_2}}{4\pi r_s^2}$$

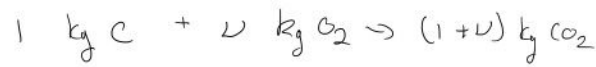
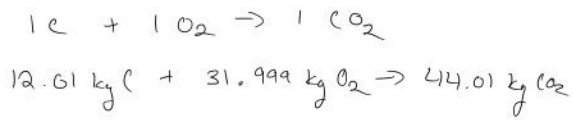
$$\dot{m}_c = \dot{m}_{CO_2} - \dot{m}_{O_2}$$

$$\dot{m}_{net}''(r) = \frac{\dot{m}_{net}}{4\pi r^2} = \frac{\dot{m}_{CO_2}}{4\pi r^2} - \frac{\dot{m}_{O_2}}{4\pi r^2}$$

$$\dot{M}_{net} = \dot{m}_{CO_2} - \dot{m}_{O_2}$$

$$\dot{m}_c'' = \dot{m}_{net}'' = \dot{m}_{CO_2}'' - \dot{m}_{O_2}''$$

just carbon surface:



$$\nu = \frac{31.999 \text{ kg O}_2}{12.01 \text{ kg C}} = 2.664 = \nu_1$$

$$\dot{m}_{\text{O}_2} = \nu_1 \dot{m}_\text{C}$$

$$\dot{m}_{\text{CO}_2} = (1+\nu_1) \dot{m}_\text{C}$$

Fick Law:

$$\dot{m}_{\text{O}_2}'' = Y_{\text{O}_2} (\dot{m}_{\text{O}_2}'' + \dot{m}_{\text{CO}_2}'') - \rho D \frac{dY_{\text{O}_2}}{dr}$$

$$\dot{m}_{\text{O}_2}'' = \frac{\dot{m}_{\text{O}_2}}{4\pi r^2} = \frac{-\nu_1 \dot{m}_\text{C}}{4\pi r^2}$$

$$\dot{m}_{\text{CO}_2}'' = \frac{\dot{m}_{\text{CO}_2}}{4\pi r^2} = \frac{\dot{m}_\text{C}(\nu_1+1)}{4\pi r^2}$$

$$\frac{-\nu_1 \dot{m}_\text{C}}{4\pi r^2} = Y_{\text{O}_2} \left(\frac{-\nu_1 \dot{m}_\text{C}}{4\pi r^2} + \frac{(\nu_1+1) \dot{m}_\text{C}}{4\pi r^2} \right) - \rho D \frac{dY_{\text{O}_2}}{dr}$$

$$-\nu_1 \dot{m}_\text{C} = \dot{m}_\text{C} Y_{\text{O}_2} - 4\pi r^2 \rho D \frac{dY_{\text{O}_2}}{dr}$$

$$-\dot{m}_\text{C} = \dot{m}_\text{C} \left(\frac{Y_{\text{O}_2}}{\nu_1} \right) - 4\pi r^2 \rho D \frac{d(Y_{\text{O}_2}/\nu_1)}{dr}$$

$$\dot{m}_\text{C} = \frac{4\pi r^2 \rho D}{1 + (Y_{\text{O}_2}/\nu_1)} \frac{d(Y_{\text{O}_2}/\nu_1)}{dr}$$

B.C.'s:

$$Y_{\text{O}_2}(r_s) = Y_{\text{O}_2,s}$$

$$Y_{\text{O}_2}(r \rightarrow \infty) = Y_{\text{O}_2,\infty}$$

$$\dot{m}_\text{C} = 4\pi r_s \rho D \ln \left[\frac{1 + Y_{\text{O}_2,\infty}/\nu_1}{1 + Y_{\text{O}_2,s}/\nu_1} \right]$$

Surface kinetics

$$R_\text{C} = \dot{m}_{\text{C},s}''' = k_\text{c} M W_\text{C} [\text{O}_2,s]$$

$$[\text{O}_2,s] = \frac{M W_{\text{mx}} P}{R_u T_s} \left(\frac{Y_{\text{O}_2,s}}{M W_{\text{O}_2}} \right)$$

$$\dot{m}_{\text{C},s}''' = k_\text{c} \frac{M W_\text{C} M W_{\text{mx}}}{M W_{\text{O}_2}} \frac{P}{R_u T_s} Y_{\text{O}_2,s}$$

$$\dot{m}_{\text{C},s}''' = \underbrace{4\pi r_s^2 k_\text{c} \frac{M W_\text{C} M W_{\text{mx}}}{M W_{\text{O}_2}} \frac{P}{R_u T_s}}_{k_{\text{loc}}} Y_{\text{O}_2,s}$$

Circuit Analogy

$$\text{Ohm's law} \quad I = \frac{\Delta V}{R}$$

by analogy $\dot{m}_c = K_{kin} Y_{O_2,s} = \frac{(Y_{O_2,s} - 0)}{1/K_{kin}} = \frac{\Delta Y}{R_{kin}}$

$$\dot{m}_c = 4\pi r_s \rho D \ln \left[1 + \frac{Y_{O_2,\infty} - Y_{O_2,s}}{Y_{O_2,s} + U_1} \right]$$

$$B_{O_2,\infty} = \text{transfer}^* = \frac{Y_{O_2,\infty} - Y_{O_2,s}}{Y_{O_2,s} + U_1}$$

$$\dot{m}_c = 4\pi r_s \rho D \ln [1 + B_{O_2,\infty}]$$

B_{O_2} is small:

$$\ln(1 + B_{O_2,\infty}) \approx B_{O_2,\infty} - \frac{1}{2} B_{O_2,\infty}^2 + \frac{1}{3} B_{O_2,\infty}^3 \dots \approx B_{O_2,\infty}$$

$$U_1 = 2.664$$

$$Y_{O_2,\infty} = 0.233 \text{ (air)}$$

$$Y_{O_2,s} = 0 - 0.233 \text{ (range)}$$

$$Y_{O_2,s} = 0: \ln(1 + B_{O_2,\infty}) = 0.0835$$

$$B_{O_2,\infty} = 0.0875$$

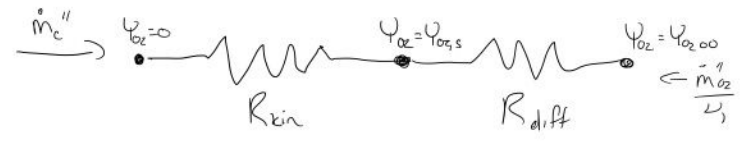
$$Y_{O_2,s} = 0.233: \ln(1 + B_{O_2,\infty}) = 0$$

$$B_{O_2,\infty} = 0$$

$$\dot{m}_c = 4\pi r_s \rho D (Y_{O_2,\infty} - Y_{O_2,s})$$

$$\dot{m}_c = \frac{4\pi r_s \rho D}{U_1 + Y_{O_2,s}} (Y_{O_2,\infty} - Y_{O_2,s})$$

$\underbrace{\hspace{10em}}_{1/R_{diff}} \quad \underbrace{\hspace{10em}}_{\Delta Y}$



$$\dot{m}_c = \frac{(Y_{O_2,\infty} - 0)}{R_{kin} + R_{diff}}$$

$$R_{kin} = 1/K_{kin} = \frac{U_1 R_s T_s (M_{O_2}/M_{mix})}{4\pi r_s^2 M_{mix} k_c \rho}$$

$$R_{diff} = \frac{U_1 + Y_{O_2,s}}{\rho D 4\pi r_s}$$

limiting cases:

$R_{kin} \ll R_{diff} \rightarrow$ diffusion controlled

$R_{diff} \ll R_{kin} \rightarrow$ kinetically controlled

regime	R_{kin}/R_{diff}	Burning Rate law
diffusive controlled	$\ll 1$	$\dot{m}_c = Y_{O_2,\infty}/R_{diff}$ $r_s \uparrow T_s \uparrow P \uparrow$
kinetics controlled	$\gg 1$	$\dot{m}_c = Y_{O_2,\infty}/R_{kin}$ $r_s \downarrow T \downarrow P \downarrow$

n be-tween

~ 1

$$v_m c = T_{0c, \infty} / (R_{kn} + R_{diff})$$